

t-test for β_3

PRS 1: In lab, you estimated the following model:

$$\text{Sales} = 17377 - 3865 \text{ prose} + 2243 \text{ pcarn} - 32.3 \text{ dinc} + 492 \text{ d2} + 331 \text{ prosed2}$$

$H_0: \beta_3 = 0$
 $H_A: \beta_3 > 0$

Is the effect of disposable income (dinc) statistically significant at the 10% level of significance?

$H_0: \beta_3 = 0$
 $H_A: \beta_3 \neq 0$

1. Yes – it has a statistically significant negative effect.
2. Yes – the estimated effect of “dinc” is statistically different from zero.
3. No – the estimated effect of “dinc” is not statistically different from zero.
4. No – the estimated effect of “dinc” is not statistically less than zero.

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Step 1: $H_0: \beta_3 = 0; H_A: \beta_3 \neq 0$

Step 2: $\alpha = 0.10$

Step 3: $t_{(0.05, 10)} = 1.812$

Step 4: $t_{\text{calc}} = -1.31$

Step 5: Conclusion – compare \rightarrow FTR

Step 6: $\hat{\beta}_3 (-32.3)$ is not statistically diff. from zero.

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V. Extensions of Multiple Regression

A. Dummy Variables

1. **Definition:** A *binary variable* that indicates a quality, condition, characteristic, etc. exists.
2. **Examples:** Cross-Section; Time-Series.
3. **Uses for Dummy Variables**
 - a. Shifting the Intercept
 - * b. Shifting the Slope *(had an intercept shift.)*
 \hookrightarrow include an interaction - just the multi. of DV and another indep. variable
4. **Interpretation**

"potential experience"

Regression Analysis: wage versus yrsed, exp, f, fexp

The regression equation is

$$\text{wage} = -4.66 + 1.49\text{yrsed} + 0.155\text{exp} - 1.03f - 0.048\text{fexp}$$

age - 6 - yrsed = exp

Predictor	Coef	SE Coef	T	P
Constant	-4.657	2.184	-2.13	0.033
yrsed	1.4850	0.1499	9.91	0.000
exp	0.15522	0.03771	4.12	0.000
f	-1.031	1.311	-0.79	0.432
fexp	-0.04778	0.05348	-0.89	0.372

interaction variable - f x exp

Two regressions:

If $f=0$:

$$\text{wage} = -4.66 + 1.49\text{yrsed} + 0.155\text{exp}$$

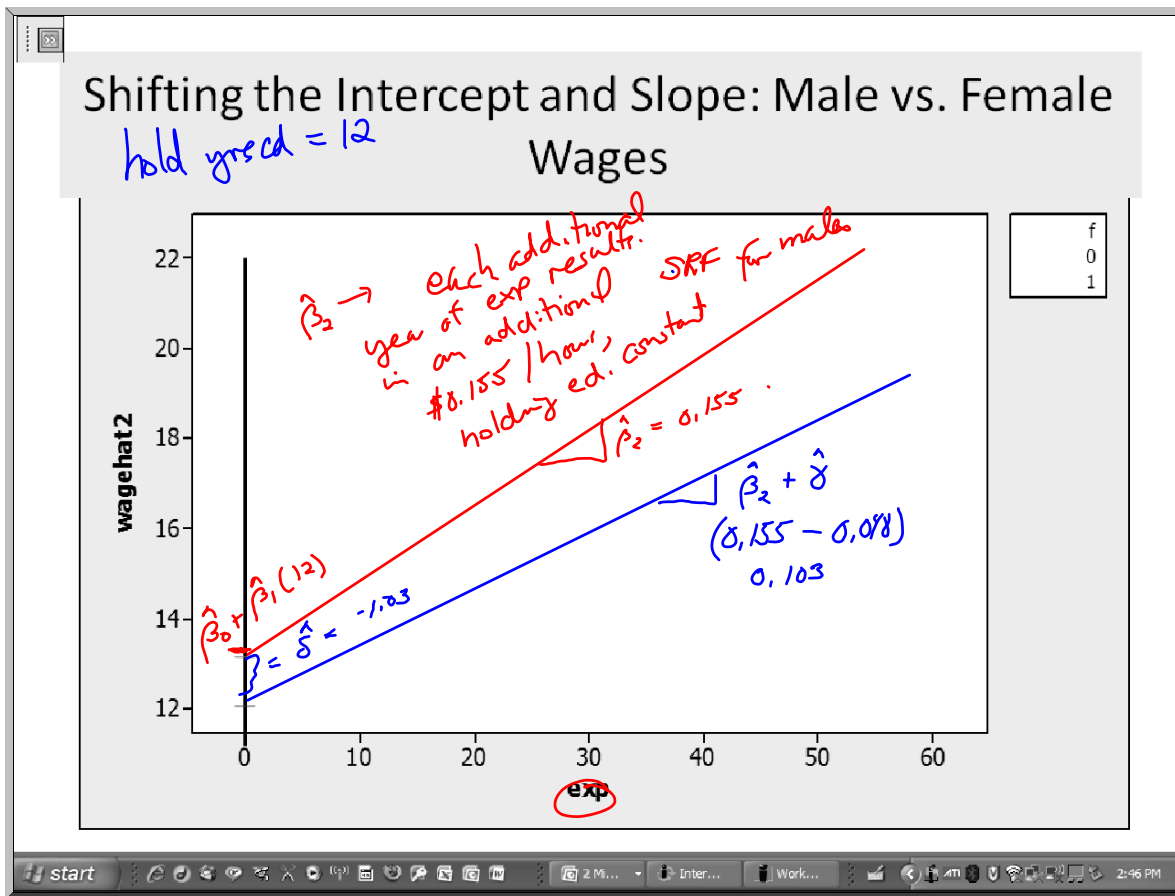
If $f=1$: *new intercept for females*

$$\text{wage} = (-4.66 - 1.03) + 1.49\text{yrsed} + (0.155 - 0.048)\text{exp}$$

new slope for females

1 value for exp

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PRS 2: The following wage equation was estimated. Wage is in \$/hour, education (Ed) and experience (Exp) are measured in years. The dummy variable F is 1 if the individual is female, 0 if male.

$$\text{Wagehat} = -5.40 + 1.45 \text{ Ed} + 0.27 \text{ Exp} - 2.92 \text{ F} - 0.09 \text{ Exp} * \text{F}$$

$F=1 \Rightarrow \text{slope } \frac{\partial \text{wage}}{\partial \text{exp}} \Big|_{F=1} = 0.27 - 0.09 = 0.18/\text{hour}$

$\hat{\beta}_2 + \hat{\delta} = 0.27 - 0.09 = 0.18/\text{hour}$

The effect of an additional year of experience on female wages is \$ ____ per hour, holding education constant.
Use 2 decimals in answering.

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4. Interpretations

- Model:

$$Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \delta D_i + \gamma (X_{1i} D_i) + u_i$$

- The parameter δ :

The effect of the dummy variable on the intercept.

Difference in the intercepts for group where $D=1$
vs. group where $D=0$

Eg. in lab - time-series dummy 1 if Q2 \Rightarrow how much different
is the intercept in Q2 versus Qs 1, 3 - 4.

is Wage - difference in intercepts for