Wavelet-Based Semantic Features for Hyperspectral Signature Discrimination

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Abstract

Hyperspectral signature classification is a quantitative analysis approach for hyperspectral imagery which performs detection and classification of the constituent materials at the pixel level in the scene. The classification procedure can be operated directly on hyperspectral data or performed by using some features extracted from the corresponding hyperspectral signatures containing information like the signature’s energy or shape. In this paper, we describe a technique that applies non-homogeneous hidden Markov chain (NHMC) models to hyperspectral signature classification. The basic idea is to use statistical models (such as NHMC) to characterize wavelet coefficients which capture the spectrum semantics (i.e., structural information) at multiple levels. Experimental results show that the approach based on NHMC models can outperform existing approaches relevant in classification tasks.

Keywords: Classification, Hyperspectral Signatures, Semantics, Wavelet, Hidden Markov Model

1. Introduction

Hyperspectral remote sensors collect reflected image data simultaneously in hundreds of narrow, adjacent spectral bands, forming a hyperspectral image cube consisting of a sequence of 2-D grayscale images where each such image is obtained at a specific spectral band [1]. For each pixel, an almost continuous spectrum curve can be derived [2], which can be referred to as a hyperspectral signature. The structure of such curve characterizes the on-ground (or near ground) constituent materials in a single remotely sensed pixel. The four major applications in the hyperspectral image literature are target detection, change detection, classification, and estimating the fraction of each material presented in the scene [2]. In this paper, we will focus on the problem of hyperspectral signature classification.

The identification of ground materials from hyperspectral images often requires comparing the reflectance spectra of the image pixels, extracted endmembers, or ground cover exemplars to a training library of spectra.
obtained in the laboratory from well characterized samples. There is a rich literature on hyperspectral image classification in the last decade, including schemes based on Scale-invariant Feature Transform (SIFT) [3], parsimonious Gaussian process models [4], and dictionary learning for sparse representations [5, 6]. For a more detailed survey on hyperspectral image classification, we refer readers to [7]. Nonetheless, classification methods emphasizing matching to a spectral library and material identification have received less attention [8–10]. On the one hand, many methods rely on nearest neighbor classification schemes based on one of many possible spectral similarity measures to match the observed test spectra with training library spectra. On the other hand, practitioners have designed feature extraction schemes that capture relevant information, in conjunction with appropriate similarity metrics, in order to discriminate between different materials.

Classification methods based on spectral similarity measures can provide researchers with simple implementation and relatively small computational requirements; however, there is a tradeoff with the amount of storage required for the training spectra as well as with the uneven performance of nearest neighbor methods. High-dimensional hyperspectral data can often be shown to be well modeled by a lower dimensional structure [11], where the lower dimensional structure is specific to each dataset. Therefore, in some cases taking the whole spectrum into consideration brings a large amount of redundant information to practitioners, while the role of relevant structural features is weakened. To ameliorate this issue, we will consider imparting different weights for different wavelengths of the spectrum in the design of the classification features.

Practitioners recognize several structural features in the spectral curves of each material as “diagnostic” or characteristic of its chemical makeup, such as the position and shape of absorption bands. Several approaches like the Tetracorder [12] have been proposed to encode such characteristics. However, such techniques require the construction of ad-hoc rules to characterize instances of each material while new rules must be created when spectral species which were not previously analyzed are added. Parente et al. [13] proposed an approach using parametric models to represent the absorption features. However, it still requires the construction of specific rules to match observations to a training library.

In this paper, we consider the formulation of an information extraction process from hyperspectral signatures via the use of mathematical models for hyperspectral signals. Our goal is to encode the signature’s scientifically meaningful structural features into numerical features, which are referred to as semantic features, without ad-hoc rules for the spectra of any material type. Our proposed method provides automated extraction of semantic information from the hyperspectral signature, in contrast with the aforementioned diagnostic characteristics designed by hand by expert practitioners. Furthermore, no new rules should need to be constructed when mineral species which were not analyzed before are added.

Mathematical signal models have been used to represent reflectance spectra. More specifically, models leveraging wavelet decompositions are of particular interest because they enable the representation of structural features at different scales. The wavelet transform is a popular tool in many signal processing
applications due to the capability of wavelet coefficients to characterize signal discontinuities at different scales and offsets. As mentioned above, the semantic information utilized by researchers is heavily related to the shape of reflectance spectra, which is succinctly represented in the magnitudes of its wavelet coefficients. A coefficient with large magnitude generally indicates a rapid change in its support while a small wavelet coefficient generally implies a smooth region. Existing wavelet approaches are limited to filtering techniques but do not extract features [8, 9].

In this paper, we apply hidden Markov models (HMMs) to the wavelet coefficients derived from the observed hyperspectral signals so that the correlations between wavelet coefficients at adjacent scales can be captured by the models. The HMMs allow us to identify significant vs. nonsignificant portions of the hyperspectral signatures with respect to the database used for training. The applications of HMMs for this purpose is inspired by the hidden Markov tree (HMT) model proposed in [14]. As for the wavelet transform, we use an undecimated wavelet transform (UWT) in order to obtain maximum flexibility on the set of scales and offsets (spectral bands or wavelengths\(^1\)) considered.

Our model for a spectrum encompassing \(N\) spectral bands takes the form of a collection of \(N\) non-homogeneous hidden Markov chains (NHMCs), each corresponding to a particular spectral band. Such a model provides a map from each signal spectrum to a binary space that encodes the structural features at different scales and wavelengths, effectively representing the semantic features that allow for the discrimination of spectra. To the best of our knowledge, the application of statistical wavelet models to the automatic selection of semantically meaningful features in hyperspectral signatures has not been proposed previously.

This paper is organized as follows. Section 2 introduces the mathematical background behind our hyperspectral signature classification system and reviews relevant existing approaches for the hyperspectral classification task. Section 3 provides an overview of the proposed feature extraction method, including details about the choice of mother wavelet, statistical model training, and label computing; we also show examples of the semantic information in hyperspectral signatures captured by the proposed features. Section 4 describes our experimental test setup as well as the corresponding results. Finally, some conclusions are provided in Section 5.

2. Background and Related Work

In this section, we begin by discussing several existing spectral matching approaches. Then, we review the theoretical background for our proposed hyperspectral signature classification system, including wavelet analysis, hidden Markov chain models, and the Viterbi algorithm.

\(^1\)We use these three equivalent terms interchangeably in the sequel.
2.1. Spectral Matching Measures

A direct comparison of spectral similarity measures taken on the observed hyperspectral signals is the easiest and the most direct way to do spectral matching. Generally speaking, spectral similarity measures can be combined with nearest neighbor classifiers. In this paper we use four commonly used spectral similarity measures. To present these measures, we use \( r_i = (r_{i1}, r_{i2}, ..., r_{iN})^T \) and \( r_j = (r_{j1}, r_{j2}, ..., r_{jN})^T \), to denote the reflectance or radiance signatures of two hyperspectral image pixel vectors.

2.1.1. Spectral Angle Measure

The spectral angle measure (SAM) \[15\] between two reflectance spectra is defined as

\[
\text{SAM}(r_i, r_j) = \cos^{-1}\left( \frac{\langle r_i, r_j \rangle}{\sqrt{||r_i||^2||r_j||^2}} \right).
\]

A smaller spectral angle indicates larger similarity between the spectra.

2.1.2. Euclidean Distance Measure

The Euclidean distance measure (ED) \[16\] between two reflectance spectra is defined as \( ED(r_i, r_j) = ||r_i - r_j||_2 \). As with SAM, smaller ED implies larger similarity between two vectors. The ED measure takes the intensity of two reflectance spectra into account, while the former is invariant to intensity.

2.1.3. Spectral Correlation Measure

The spectral correlation measure (SCM) \[17\] between two reflectance spectra is defined as

\[
\text{SCM}(r_i, r_j) = \frac{\sum_{k=1}^{N}(r_{ik} - \bar{r}_i)(r_{jk} - \bar{r}_j)}{\sqrt{\sum_{k=1}^{N}(r_{ik} - \bar{r}_i)^2 \sum_{k=1}^{N}(r_{jk} - \bar{r}_j)^2}}.
\]

where \( \bar{r}_i \) is the mean of the values of all the elements in a reflectance spectrum vector \( r_i \). The SCM can take both positive or negative values; larger positive values are indicative of similarity between spectra.

2.1.4. Spectral Information Divergence Measure

The spectral information divergence measure (SID) \[18\] between two reflectance spectra is defined as \( \text{SID}(r_i, r_j) = D(r_i||r_j) + D(r_j||r_i) \), where \( D(r_i||r_j) \) is regarded as the relative entropy (or Kullback-Leibler divergence) of \( r_j \) with respect to \( r_i \), which is defined as

\[
D(r_i||r_j) = -\sum_{k=1}^{N} p_{ik} (\log p_{jk} - \log p_{ik}).
\]

Here \( p_{ik} = r_{ik}/\sum_{k=1}^{N} r_{ik} \) corresponds to a normalized version of the spectrum \( r_i \) at the \( k \)th spectral band, which is interpreted in the relative entropy formulation as a probability distribution.
2.2. Wavelet Analysis

The wavelet transform of a signal provides a multiscale analysis of a signal’s content which effectively encodes in a compact fashion the locations and scales at which the signal structure is present [19]. To date, several hyperspectral classification methods based on wavelet transform have been proposed. Most of these classification approaches (e.g. [10, 20, 21]) employ a dyadic/decimated wavelet transform (DWT) as the preprocessing step. Compared with UWT, the DWT provides a more concise representation because it minimizes the amount of redundancy in the coefficients. However, the tradeoff for such redundancy is that UWT provides maximum flexibility on the choice of scales and offsets used in the multiscale analysis, which is desired because it allows for a simple characterization of the spectrum structure at each individual spectral band.

A one-dimensional real-valued UWT of an \( N \)-sample signal \( x \in \mathbb{R}^N \) is composed of wavelet coefficients \( w_{s,n} \), each labeled by a scale \( s \in 1, ..., L \) and offset \( n \in 1, ..., N \), where \( L \leq N \). The coefficients are defined using inner products as \( w_{s,n} = \langle x, \phi_{s,n} \rangle \), where \( \phi_{s,n} \in \mathbb{R}^N \) denotes a sampled version of the mother wavelet function \( \phi \) diluted to scale \( s \) and translated to offset \( n \):

\[
\phi_{s,n}(\lambda) = \frac{1}{\sqrt{s}} \phi \left( \frac{\lambda - n}{s} \right),
\]

where \( \lambda \) is a scalar. Each coefficient \( w_{s,n} \), where \( s < L \), has a child coefficient \( w_{s+1,n} \) at scale \( s + 1 \). Similarly, each coefficient \( w_{s,n} \) at scale \( s > 1 \) has one parent \( w_{s-1,n} \) at scale \( s - 1 \). Such a structure in the wavelet coefficients enables the representation of fluctuations in a spectral signature by chains of large coefficients appearing within the columns of the wavelet coefficient matrix \( W \).

2.3. Advantages of Haar Wavelet

The Haar wavelet is the simplest possible compact wavelet which has the properties of square-like shape and discontinuity. These properties makes the Haar wavelet sensitive to a larger range of fluctuations than other mother wavelets and provides it with a lower discriminative power. Thus, the Haar wavelet enables the detection of both slow-varying fluctuations and sudden changes in a signal [19], while not particularly sensitive to small discontinuities (i.e., noise) on a signal, in effect averaging them out over the wavelet support.

Consider the example in Fig. 2.3, where the figure at the top represents an example hyperspectral signature, while the figures in the middle and at the bottom show the undecimated wavelet coefficient matrix of the spectrum under the Haar and Daubechies-4 wavelets, respectively. The middle figure in Fig. 2.3 shows the capability of Haar wavelets to capture both rapid changes and gently sloping fluctuations in the sample reflectance spectrum. Similarly, the bottom figure shows that the Daubechies-4 wavelet is sensitive to compact and drastic discontinuities (i.e., higher order fluctuations that are often due to noise). Thus, the Daubechies-4 wavelet does not provide a good match to semantic information extraction for this
example reflectance spectrum. Intuitively, these issues will also be present for other higher-order wavelets, which provide good analytical matches to functions with fast, high-order fluctuations.

In general, wavelet representations of spectral absorption bands are less emphasized under Haar wavelet than under other higher order wavelets. However, this drawback can be alleviated using discretization, which will be described in the next subsection.

2.4. Statistical Modeling of Wavelet Coefficients

The pairwise statistics of DWT coefficients can be succinctly captured by a hidden Markov model [14]. The dyadic nature of DWT coefficients gives rise to a hidden Markov tree (HMT) model that characterizes the clustering and persistence properties of wavelet coefficients. The statistical model is constructed based on the wavelet representation of spectra in a training library.

The statistical model is driven by the energy compaction property of the DWT. This property motivates the use of a zero-mean Gaussian mixture model (GMM) with two Gaussian components. The first Gaussian component features a high variance and characterizes the small number of “large” coefficients; thus, this state is labeled L. The second Gaussian component features a low variance and characterizes the large number of “small” wavelet coefficients; thus, this state is labeled S. More precisely, the conditional probability of a wavelet coefficient \( w_s \) given the value of the state \( S_s \) can be written as \( p(w_s|S_s = i) = \mathcal{N}(0, \sigma^2_{i,s}) \), where \( i = \{S, L\} \). The state \( S_s \in \{S, L\} \) of a wavelet coefficient collects these labels, and is said to be hidden because the label values are not explicitly observed. The two states are provided with likelihoods \( p_{S_s}(L) = p(S_s = L) \) and \( p_{S_s}(S) = p(S_s = S) \) such that \( p_{S_s}(L) + p_{S_s}(S) = 1 \). Consequently, the distribution of the same wavelet coefficient can be written as \( p(w_s) = p_{S_s}(L)\mathcal{N}(0, \sigma^2_{L,s}) + p_{S_s}(S)\mathcal{N}(0, \sigma^2_{S,s}) \).

\(^{1}\text{Since the same model is used for each chain of coefficients } \{S_{1,n}, \ldots, S_{L,n}\}, \text{ } n = 1, \ldots, N, \text{ we remove the index } n \text{ from the subscript for simplicity in this sequel whenever possible.}\)
UWT coefficients exhibit a persistence property [22, 23], which states that chain of wavelet coefficients at adjacent scales are consistently small or large with high probability. This property can be accurately modeled by a non-homogeneous hidden Markov chain (NHMC) that links the states of wavelet coefficients in the same offset. More specifically, the state $S_s$ of a coefficient $w_s$ is only affected by the state $S_{s-1}$ of its parent (if it exists) and by the value of its coefficient $w_s$. The Markov chain in the NHMC is parameterized by the likelihoods for the first state $P_{S_1}(L)$ and $P_{S_1}(S)$, as well as the set of state transition matrices for the different parent-child label pairs $(S_{s-1}, S_s)$ for $s > 1$:

$$A_s = \begin{pmatrix} p_{S \to S_s} & p_{L \to S_s} \\ p_{S \to L_s} & p_{L \to L_s} \end{pmatrix},$$

(1)

where $p_{i \to j, s} := P(S_s = j | S_{s-1} = i)$ for $i, j \in \{L, S\}$. The parameters for the NHMC

$$\theta = \{p_{S_1}(S), p_{S_1}(L), \{A_s\}_{s=2}^L, \{\sigma_{S,s}, \sigma_{L,s}\}_{s=1}^L\}$$

(which include the probabilities for the first hidden states, the state transition matrices, and Gaussian variances for each of the states) that maximize the likelihood of a set of observations can be obtained via the expectation maximization (EM) algorithm [14, 24].

### 2.5. Wavelet-based Spectral Matching

Many hyperspectral signature classification approaches have been proposed in the literature, with a subset of them involving wavelet analysis [8–10, 25, 26]. In this paper, we review two approaches that are particularly close in scope to our proposed method, which will be used for comparison in our numerical experiments. Since our focus in this paper is on hyperspectral classification for individual pixels, we limit our comparison to methods that rely exclusively on the spectral of a given pixel or on features obtained from the pixel’s spectra. More specifically, we do not compare to other methods that use additional information (e.g. spatial information for a HSI) or that assume prior knowledge of the location of semantic information, which is usually obtained from an expert practitioner.

First, Rivard et al. [8] propose a method based on the wavelet decomposition of the spectral data. The obtained wavelet coefficients are separated into two categories: low-scale components of power (LCP) capturing mineral spectral features (corresponding to the first fine scales), and high-scale components of power (HCP) containing the overall continuum (corresponding to coarser scales). The coefficients for the LCP spectrum, which capture detailed structural features, are summed across scales at each spectral band. This process can conceptually be described as a filtering approach, since the division into LCP and HCP effectively acts as a high-pass filter that preserves only the fine-scale detailed portion of the spectrum.

A second wavelet-based classification approach is proposed in [9]. This second approach applies an UWT on the entire database. The set of wavelet coefficients for each separate wavelength is considered as
a separate feature vector. Linear discriminant analysis (LDA) is performed on each one of these vectors for dimensionality reduction purposes. The outputs are grouped into $C$ classes, corresponding to the elements of interest, to train either a single multivariate Gaussian distribution or a GMM for each of the classes, where a classification label or score is obtained for each wavelength. Finally, decision fusion is performed among the wavelengths to obtain a single classification label for the spectrum. It is implicitly expected by this method that the number of training samples for each one of the classes is sufficiently large so that the class-specific Gaussian (mixture) models can be accurately constructed.

3. NHMC-Based Feature Extraction and Classification

In this section, we introduce a feature extraction scheme for hyperspectral signatures that exploits a Markov model for the signature’s wavelet coefficients. A wavelet analysis is used in an UWT to capture information on the fluctuations of the spectra. The state labels extracted from the Markov model represent the semantic information relevant for hyperspectral signal processing.

3.1. Semantic Features from NHMC Labels

Once the model has been trained, the value of the states $S = \{S_{l,n}\}_{l=1,...,L, n=1,...,N}$ can be estimated from the wavelet coefficients $\{w_{l,n}\}_{l=1,...,L, n=1,...,N}$ of the spectrum $x$ using a Viterbi algorithm \[14\] \[27\].

We collect the states into an $L \times N$ array $S$ to obtain a semantic feature vector for the spectrum $x$: states labeled as “large” describe statistically significant fluctuations in the spectrum at the given band and scale,
while states labeled as “small” describe either the lack of fluctuation or lack of statistical significance of
the fluctuation over the training set. An example is shown in Figure 2, showing that large state labels
correspond to statistically meaningful fluctuations in the spectrum of a sample of ilmenite.

Figure 2 shows, however, that the state label itself does not encode information about the direction in
which the fluctuation occurs. Luckily, we find that this information can be easily extracted from the wavelet
coefficient vector, when the Haar wavelet is used in the UWT [19]. Therefore, we choose to augment the
state array \( S \) by endowing each state label with the sign of the corresponding wavelet coefficient.

### 3.2. Multi-State Hidden Markov Chain Model

In our system, we choose to use the NHMC model described in Section 2.4 applied to the UWT via the
Haar wavelet. We select the Haar wavelet due to its special shape, which allows for the magnitude of the
wavelet coefficients to be proportional to the slope of the spectra across the wavelet’s support. Furthermore,
the signs of these coefficients are indicative of the slope orientation (increasing or decreasing for negative
and positive, respectively).

In contrast to the prior work of [14], the NHMC approach we use here features \( k \)-state GMMs, with \( k > 2 \), to model each wavelet coefficient. Our simulations have shown that the NHMC model with \( k = 2 \)
provides state labels with an overly coarse distinction between fluctuations and flat regions, which often
neglects to capture the presence of absorption bands (in particular weak bands); such bands often do
provide discriminants between mineral classes, and the performance of classification improves with larger
values of \( k \), as will be shown in the sequel.

We associate each wavelet coefficient \( w_s \) with an unobserved hidden state \( S_s \in \{0, 1, ..., k - 1\} \), where
the states have prior probabilities \( p_{i,s} := p(S_s = i) \) for \( i = 0, 1, ..., k - 1 \). Here the state \( i = 0 \) represents
smooth regions of the spectral signature, in a fashion similar to the small (S) state for binary GMMs,
while \( i = 1, ..., k - 1 \) represent a more finely grained set of states for spectral signature fluctuations,
similarly to the large (L) state in binary GMMs. All the weights should meet the condition \( \sum_{i=0}^{k-1} p_{i,s} = 1 \).
Each state is characterized by a zero-mean Gaussian distribution for the wavelet coefficient with variance
\( \sigma_{i,s}^2 \). The value of \( S_s \) determines which of the \( k \) components of the mixture model is used to generate the
probability distribution for the wavelet coefficient \( w_s \): \( p(w_s|S_s = i) = N(0, \sigma_{i,s}^2) \). We can then infer that
\[
p(w_s) = \sum_{i=0}^{k-1} p_{i,s} p(w_s|S_s = i).
\]
In analogy with the binary GMM case, we can also define a \( k \times k \) transition probability matrix
\[
A_s = \begin{pmatrix}
  p_{0\rightarrow0,s} & p_{1\rightarrow0,s} & \cdots & p_{k-1\rightarrow0,s} \\
p_{0\rightarrow1,s} & p_{1\rightarrow1,s} & \cdots & p_{k-1\rightarrow1,s} \\
\vdots & \vdots & \ddots & \vdots \\
p_{0\rightarrow k-1,s} & p_{1\rightarrow k-1,s} & \cdots & p_{k-1\rightarrow k-1,s}
\end{pmatrix},
\]
where $p_{i\rightarrow j,s} = p(S_s = j|S_{s-1} = i)$. Note that the probabilities in the diagonal of $A_s$ are expected to be larger than those in the off-diagonal elements due to the persistence property of wavelet transforms. Note also that all state probabilities $p_{i,s}$ for $s > 1$ can be derived from the matrices $\{A_s\}_{s=2}^L$ and $\{p_{i,1}\}_{i=0}^{k-1}$.

3.3. Additional Modifications to NHMC

Unfortunately, a large number of GMM states might also have negative influence in semantic modeling due to spectral variability, i.e., to the diversity of reflectance values for different bands. More specifically, we see in our experiments that the maps from rates of fluctuation to the $k$ available state labels may be significantly different for wavelet coefficients corresponding to neighboring bands. Although we observe that the lowest variance state is consistently assigned to bands without statistically significant fluctuations, the assignment of $k$-ary labels to fluctuations at different bands is not nearly as uniform, making the evaluation of the spectral signature from the semantic features more difficult.

Figure 3 provides an example comparison between labels obtained from the $k$-state GMM NHMC and the MOG-NHMC; the figure highlights the variability obtained when $k$ labels are used in the feature, reducing its semantic significance, while MOG-NHMC retains semantic significance.

3.4. Illustration of Extracted Semantic Information

We have observed four distinct behaviors of hyperspectral signatures that are captured by the MOG-NHMC semantic features proposed above: (i) the direction of fluctuation in the reflectance spectra, which is captured in the state label values; (ii) the width of the fluctuation, which is captured by the width of
Figure 4: Semantic information extracted in some sample spectral curves based on MOG with 2 states. Top row: Sample spectral curves with extracted semantic information. Bottom row: corresponding state label array.

a sequence of matching labels through neighboring wavelengths; (iii) the slope of the fluctuation, which is captured by the number of matching state values through the scales at the given spectral band; and (iv) the locations of the absorption bands, which are captured by the band indices at which the feature switch from -1 to 1 or vice-versa. Figure 4 illustrates these four types of captured information in several example reflectance spectra. First, we transform the state array $S$ into a vector $S_v$ by collecting the most prevalent state for each band (i.e., the state that appears most often in each column of $S$). We show four example reflectance spectra that are colored according to the state vector $S_v$ (green, red, and blue for 0, +1, and −1, respectively). The bands for which $S_v$ fluctuates from 1 to -1 are labeled to identify the location of absorption minima. This representation can be considered a summary of the semantic information in the spectra, equivalent to renditions such as the ones used by practitioners for automatic mineral identification. The difference is that the semantic features in the NHMC approach are extracted directly from the data and not defined a priori by an expert.

3.5. NHMC Classification Summary

We provide an overview of the NHMC-based hyperspectral classification system in Fig. 5. The system consists of two modules: an NHMC model training module and a classification module. The training stage uses a training library of spectra containing samples from the classes of interest to train the NHMC model, which is then used to compute state estimates for each of the training spectra using a Viterbi Algorithm. The state arrays obtained from the NHMC model will then be used as classification features coupled with a classification scheme, e.g., nearest-neighbor (NN) or support vector machine (SVM) classification. The testing module considers a spectrum under test and computes the state estimates under the trained NHMC model using the parameters obtained during training. The module then applies the classification scheme.
4. Classification Experiments and Result Analysis on Synthetic Data

In this section, we present multiple experimental results that assess the performance of the proposed features in hyperspectral signature classification. We also study the effect of NHMC parameter selections on the classification performance from the corresponding extracted features.

4.1. Study Data and Performance Evaluation

Our simulations use the RELAB spectral database with 26 mineral reflectance spectrum classes. To select a uniform range of wavelength for all spectra used, we focus on the spectral region 0.35 \( \mu \)m to 2.6 \( \mu \)m corresponding to most of the visible and near-infrared region of the electromagnetic spectrum. The spectral sampling step is 5 nm. The classes selected exhibit each a different number of measured spectra; therefore, in order to avoid possible estimation biases in the NHMC and classifier training, we generate new samples for each class by applying the Hapke mixing model \[28\] to existing samples with randomly selected mixture weights in order to increase the number of samples for each class to match the largest available (65). The resulting dataset contains 1690 reflectance spectra that are normalized as well to remove the effect of varying illumination conditions in classification.
We compare the proposed NHMC models: the different instances of the model we test use \( k = 2 \) to 10 classes, with and without MOG conversion and wavelet coefficient sign augmentation. Our training/testing datasets are obtained by a random 80%/20% partition for training and testing uniformly for each class selected. Unfortunately, we observe that the classes in the resulting dataset are almost perfectly well separated, making it difficult to differentiate between the proposed models in terms of performance as they are near perfect for all. We therefore consider a more difficult problem that aims at identifying dominant elements in material mixtures in a hyperspectral image where the pixels correspond to the testing sample described earlier under a randomized 2-D assignment to pixels. The mixtures are introduced to mimic an image formation process that includes spatial blurring with a \( 3 \times 3 \) Gaussian kernel, with the center pixel corresponding to the dominant material and defining the sought label. The difficulty of the resulting classification process is controlled in terms of the variance of the Gaussian blurring kernel, and is measured in terms of the dominant material percentage (DMP), i.e., the weight of the center pixel in the blurring kernel. In our experiment, we vary the DMP from 70\% to 100\% with a step of 5\%.

### 4.2. Feature Comparison

For this study, classification performance is evaluated by using NN and SVM classification accuracies. For the NN classifier, three distance metrics are employed: \( \ell_1 \) distance, Euclidean (\( \ell_2 \)) distance, and cosine similarity measure. For the SVM classifier, we use radial basis function (RBF) as the kernel and perform a grid search for the corresponding parameter values (cost and Gaussian variance) that provide best performance for each NHMC model. Both the NHMC model (if applicable) and the classifier (NN or SVM) are trained using the aforementioned training set, and the performance is measured on the aforementioned test set.

Figure 6 shows the classification rates for different NHMC models under different dominant material percentages using the aforementioned NN and SVM classifiers. Additionally, the figure also includes the classification accuracies of the related approaches described in Section 2.5. In the figure, different classification features are identified as follows: “Rivard” denotes the approach proposed in [8]; “Wavelet Coefficient” denotes the classification scheme of using wavelet coefficients as classification features; “Spectral Similarity” denotes spectral similarity matching classification scheme (i.e., the spectra themselves are the input to each NN classifier); “GMM” denotes an NHMC featuring Gaussian mixture models; “MOG” denotes an NHMC featuring mixtures of Gaussians; and “GMM+Sign” and “MOG+Sign” denotes the previous two approaches where Haar wavelet coefficient signs being added to state labels. Our NHMC tests involve NHMC models containing different numbers of mixed Gaussian components; Fig. 6 shows the highest performance among all tested values for the number of mixed Gaussian components.

Note that “Rivard” only appears in the bottom left figure of Fig. 6 because it is defined specifically in terms of a NN classifier with cosine distance [8].
Figure 6: Classification rates of different NHMC modeling approaches and other relative classification approaches under different dominant material percentages. Top left: NN classifiers with $\ell_1$ distance; top right: NN classifier with Euclidean distance; bottom left: NN classifier with cosine similarity; bottom right: SVM classifier. For NHMC models, the highest classification rate among the models tested is listed for each DMP value.

We highlight some features of the obtained results:

- In most cases, the use of signs in the NHMC features improves performance with respect to their original counterparts.

- In the NN classifiers, GMM performs better than MOG for lower DMPs, which are more challenging settings, while MOG with additional signs outperforms GMM for DMPs closer to 100%. Nonetheless, in most cases MOG without wavelet coefficient signs provides the worst performance.

- While the performance of NHMC methods with SVM classifiers is higher than that obtained with NN classifiers, they are outperformed by the wavelet coefficient approach. We conjecture that this is due to the discrete nature of NHMC labels, which are not as easily leveraged in the SVM’s search for a separation boundary from support vectors.
We also attempted to implement the approach proposed in [9]. However, because of the lack of sufficient data for individual classes, we obtained several ill-conditioned covariance matrices when constructing multivariate GMMs. Thus, we do not include the comparison with this approach in this paper.

### 4.3. NHMC Parameters

Next, we evaluate the effect of the number of states included in the NHMC model on the performance of the tested classifiers. We set the DMP to 85% for concreteness, and evaluate the classification performance of all proposed NHMC features with NN and SVM classifiers as a function of the number of states, which varies between 2 and 10 for GMM and between 3 and 10 for MOG. Fig. 7 shows the variation tendency of classification accuracy with increasing number of mixed Gaussian components using different classifiers and similarity metrics.

From these four figures, we see that MOG with additional wavelet coefficient signs provides relatively
consistent performance compared with other NHMC-based models. Additionally, in terms of classification accuracy, the two model configurations using MOG provide two performance extremes: by adding wavelet coefficient signs we obtain the highest classification performance, while MOG without signs provides the lowest one. As mentioned earlier, MOG combines the simplicity of a binary-state GMM and the spectral fluctuation characterization capability of a multistate GMM. In that case, if we do not consider the signs of the wavelet coefficient, spectra that have approximately matching locations for their fluctuations while exhibiting differing magnitudes and orientations will be matched to similar MOG label vectors. The reason is that a binary-state GMM form could assign the same state labels to several fluctuations of different levels and orientations. However, if Haar wavelet coefficient signs are added, the state labels better reflect the spectral fluctuation orientation information.

5. Conclusion

In this paper, we proposed the design of a feature extraction scheme for hyperspectral signatures that preserves the semantic information used by practitioners in signature discrimination (i.e., location of distinguishing fluctuations and discontinuities). Our approach is automated thanks to the use of statistical models for wavelet transform coefficients, which succinctly capture the location and magnitude of fluctuations in the spectra observed. Furthermore, the statistical model also enables a segmentation of the spectra into informative and non-informative portions. The success of statistical modeling is mostly dependent on the availability of a large-scale database for training containing representative examples of the spectra that are observed by the sensing system.

We also tested the quality of the preservation of semantic information in our proposed features by using a simple example hyperspectral classification system based on nearest neighbor search. We also compared our feature extraction method with three existing feature extraction approaches for classification; the first approach is spectral matching, which performs classification directly on the hyperspectral signature; the second approach performs classification directly on wavelet coefficients, and the third approach computes features as the sum of wavelet coefficients of certain scales. We showed that the performance of our proposed features meets or exceeds that of baselines relying on spectral matching and wavelet coefficient representations, in particular for high DMP.

While the performance of each method we tested decreases as the DMP is reduced, the reduction is stronger for the MOG and GMM methods in comparison with some of their counterparts (in particular, to the case where NN with cosine similarity is applied directly on the spectra). We believe that this effect is due to the additional difficulty of modeling signal classes of increased variability (as the DMP decreases) using the extracted binary features. Nonetheless, we note that even with this handicap the performance of the best combinations of NHMC features and NN classifiers exceeds the performance of the comparison baseline.
methods when the DMP is sufficiently large. Furthermore, we believe that the size of the datasets we use here, while much larger than that of our previous results [29–31], may still be insufficient to fully exploit the power of the statistical models leveraged here. Thus, further work will focus on expanding the size of database and investigating additional modifications to the feature extraction scheme and the underlying statistical models. As an example, NHMC models based on nonzero-mean GMM are an attractive alternative to be pursued in the future, as in certain cases the histogram of wavelet coefficients cannot be accurately modeled by zero-mean Gaussian mixture models.

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References


