

### Computing with ‘Logically Possible Partly-Fregean Interpretations’

Let  $h$  be the meaning assignment determined by the logically possible partly-Fregean interpretation in (53) of the handout “Fregean Interpretations.”

- (i)  $h((\lambda P_4 \exists x_3 ((\mathbf{man}' x_3) \& (P_4 x_3)))) =$  (by definition of Politics+ $\lambda$ )
- (ii)  $h(F_\lambda(P_4, F_\exists(x_3, F_{\text{And}}(F_{\text{Concat}}(\mathbf{man}, x_3), F_{\text{Concat}}(P_4, x_3))\dots))) =$  (by homomorph. of  $h$ )
- (iii)  $G_\lambda(h(P_4), G_\exists(h(x_3), G_{\text{And}}(G_{\text{Concat}}(h(\mathbf{man}), h(x_3)), G_{\text{Concat}}(h(P_4), h(x_3))\dots))) =$  (by def. of  $h$ )
- (iv)  $G_\lambda(f(P_4), G_\exists(f(x_3), G_{\text{And}}(G_{\text{Concat}}(f(\mathbf{man}), f(x_3)), G_{\text{Concat}}(f(P_4), f(x_3))\dots))) =$  (by def. of  $f$ )
- (v)  $G_\lambda(f(P_4), G_\exists(f(x_3), G_{\text{And}}(G_{\text{Concat}}(mn, f(x_3)), G_{\text{Concat}}(f(P_4), f(x_3))\dots))) =$  (by def. of  $G_\lambda$ )
- (vi) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = G_\exists(f(x_3), G_{\text{And}}(G_{\text{Concat}}(mn, f(x_3)), G_{\text{Concat}}(f(P_4), f(x_3))\dots))(g(P_4/x)) =$  (by def. of  $G_\exists$ )
- (vii) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = [\text{The function } E \text{ such that if } g' \in J, E(g') = 1 \text{ iff there is a } y \in D_{e, E} \text{ such that } G_{\text{And}}(G_{\text{Concat}}(mn, f(x_3)), G_{\text{Concat}}(f(P_4), f(x_3))\dots)(g'(x_3/y)) = 1](g(P_4/x)) =$  (by meta-logic)
- (viii) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is an  $y \in D_{e, E}$  such that  
 $G_{\text{And}}(G_{\text{Concat}}(mn, f(x_3)), G_{\text{Concat}}(f(P_4), f(x_3))\dots)(g(P_4/x)(x_3/y)) = 1 =$  (by def. of  $G_{\text{And}}$ )
- (ix) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is an  $y \in D_{e, E}$  such that  
[The function  $\text{Conj}$  such that if  $g' \in J$ , then  $\text{Conj}(g') = 1$  iff  
 $G_{\text{Concat}}(mn, f(x_3))(g') = 1$  and  $G_{\text{Concat}}(f(P_4), f(x_3))(g') = 1](g(P_4/x)(x_3/y)) = 1 =$  (by meta-logic)

- (x) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
 The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is an  $y \in D_{e, E}$  such that  
 $G_{\text{Concat}}(mn, f(x_3))(g(P_4/x)(x_3/y)) = 1$  and  $G_{\text{Concat}}(f(P_4), f(x_3))(g(P_4/x)(x_3/y)) = 1$   
 $=$  (by def. of  $G_{\text{Concat}}$ )
- (xi) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
 The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is an  $y \in D_{e, E}$  such that  
 $mn((g(P_4/x)(x_3/y))(f(x_3)(g(P_4/x)(x_3/y)))) = 1$  and  
 $f(P_4)((g(P_4/x)(x_3/y))(f(x_3)(g(P_4/x)(x_3/y)))) = 1$   $=$  (by (53))
- (xii) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
 The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is an  $y \in D_{e, E}$  such that  
 $i(g(P_4/x)(x_3/y))(x_3) = 1$  and  $g(P_4/x)(x_3/y)(P_4)(g(P_4/x)(x_3/y))(x_3) = 1$   
 $=$  (by def. of ‘Logically Possible Partly-Fregean Interpretation)
- (xiii) The function  $L$  such that if  $g \in J$ ,  $L(g) =$   
 The function  $p$  with domain  $D_{\langle e, t \rangle, E}$  such that for any  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is an  $y \in D_{e, E}$  such that  $i(y) = 1$  and  $x(y) = 1$

Thus,  $h((\lambda P_4 \exists x_3 ((\mathbf{man}' x_3) \& (P_4 x_3))))$  is computed to be a constant function on variable assignments.

- It maps every variable assignment to the function  $p$ , which is the characteristic function of the set of  $\langle e, t \rangle$  functions  $f$  which map some  $\mathbf{man}$  to 1.
- Thus, it maps every variable assignment to the ‘set of properties that some  $\mathbf{man}$  has’

Note the parallel to our model theoretic semantics from the handout “Preliminaries”:

Let  $\mathcal{M}$  be the model defined in (13) of “Preliminaries”. Let  $g$  be any variable assignment based on  $\mathcal{M}$ .

$$[[[(\lambda P_4 \exists x_3 ((\mathbf{man}' x_3) \& (P_4 x_3)))]]]^{\mathcal{M}, g} =$$

The function  $p$  with domain  $D_{\langle e, t \rangle, E}$ , range  $D_{t, E}$  and for all  $x \in D_{\langle e, t \rangle, E}$ ,  
 $p(x) = 1$  iff there is a  $y \in D_{e, E}$  such that  $i(y) = 1$  and  $x(y) = 1$